

## Index of terms used in the problems

The index is organized as follows: First come some terms that are not readily alphabetized. After that everything is in alphabetical order, with the understanding that, for example,  $\alpha$  is alphabetized as ‘alpha’, 2 as ‘two’ etc.

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